

# Cryptographic Protocols

## Exercise 11

### 11.1 Information-Theoretic Commitment Transfer Protocol

- a) Consider the information-theoretically secure (distributed) commitment scheme from the lecture. Describe the state achieved by the COMMIT protocol, i.e., describe the output of each player and the consistency condition among these outputs.
- b) Design a commitment transfer protocol CTP for a COMMIT-state. Show that your protocol is secure.

### 11.2 Information-Theoretic Commitment Multiplication Protocol

- a) Show that the commitment multiplication protocol for the generic information-theoretic secure MPC from the lecture is secure for  $t < n/3$ , i.e., that it satisfies the properties:
  1. CORRECTNESS: At the end of CMP, either the dealer  $D$  is committed to  $d$  such that  $d = ab$ , or it is publicly seen that  $D$  is corrupted.
  2. PRIVACY: Up to  $t$  players (not including  $D$ ) obtain no information on the values  $a$  and  $b$ .
- b) Show that the protocol CMP is insecure if  $t \geq n/3$ .  
HINT: Show that if  $n = 3t$ , then an adversary corrupting  $t$  players (including  $D$ ) can achieve that at the end of the protocol player  $D$  is committed to some  $d' \neq ab$ .

### 11.3 Commitment Multiplication Protocol for ElGamal

Recall the ElGamal commitment scheme. The blob function maps elements of  $\mathbb{Z}_q \times \mathbb{Z}_q$  to elements of  $G \times G$ , where  $q$  is a prime number and  $G$  is a cyclic group of order  $q$ . More concretely, it takes the value  $a \in \mathbb{Z}_q$  and randomness  $\alpha \in \mathbb{Z}_q$  and outputs a pair  $A := (g^\alpha, \gamma^a h^\alpha)$ , where  $g$ ,  $h$  and  $\gamma$  are generators of  $G$ .

Provide a commitment multiplication protocol CMP for this commitment scheme.