

# Cryptographic Protocols

## Exercise 13

### 13.1 General Adversary Structures

Consider the set of players  $P = \{P_1, \dots, P_n\}$ . As seen in the lecture, an adversary structure is a collection  $\mathcal{Z} \subseteq 2^P$ , that is closed under taking subsets. That is, if  $Z \in \mathcal{Z}$  and  $Z' \subseteq Z$  then  $Z' \in \mathcal{Z}$ . An adversary structure  $\mathcal{Z}$  is  $Q^k$  if no  $k$  sets in  $\mathcal{Z}$  cover  $P$ . The maximal sets of an adversary structure  $\mathcal{Z}$  are the elements  $Z \in \mathcal{Z}$  such that no  $Z' \supset Z$  is in  $\mathcal{Z}$ .

- a) Compute the adversary structure induced by the threshold condition  $t < n/3$ . What is the number of maximal sets?
- b) Show that if there is a protocol  $\pi$  actively secure against an adversary structure that is not  $Q^3$ , then there is a protocol  $\pi'$  that is actively secure in the threshold setting for  $n = 3$  and  $t = 1$ .
- c) Give a  $Q^3$ -adversary structure  $\mathcal{Z}$  for  $n = 6$  that contains a set of 3 parties.

### 13.2 Weak Consensus for GA

In the lecture it was mentioned that there are actively secure broadcast protocols against  $Q^3$ -adversaries. One can adapt the consensus protocol from the lecture to be secure against general adversaries.

Adjust the protocol for weak consensus from the lecture to be secure against  $Q^3$ -adversaries characterized by  $\mathcal{Z}$ .

### 13.3 Active Multiplication Protocol

Prove that the active multiplication protocol seen in the lecture is secure. In particular, show that privacy and correctness are satisfied.